

**PART : PHYSICS**

1. A drop of radius  $R$  is split into 27 drops of equal radius, the work done is 10 J. If the same big drop is split into 64 equal drops the work done is-

(1) 10 J                      (2) 15 J                      (3) 20 J                      (4)  $\frac{75}{4}$  J

**Ans. (2)**

**Sol.**  $27 \times \frac{4}{3} \pi r^3 = \frac{4}{3} \pi R^3$

$$r = \frac{R}{3}$$

initial surface area =  $4\pi R^2$

Final surface area =  $4\pi r^2 \times 27$

Change in surface area =  $4\pi (27r^2 - R^2)$

$$= 4\pi \left( 27 \left( \frac{R}{3} \right)^2 - R^2 \right) = 8\pi R^2$$

Work done by External Agent =  $T \times 8\pi R^2 = 10$  ..... (i)

$$64 \times \frac{4}{3} \pi r^3 = \frac{4}{3} \pi R^3 \Rightarrow r = \frac{R}{4}$$

change in surface area =  $4\pi (64r^2 - R^2)$

$$= 4\pi \left( 64 \left( \frac{R}{4} \right)^2 - R^2 \right)$$

$$= 12\pi R^2$$

Work done by External Agent =  $T \times 12\pi R^2 = 12 \times \frac{10}{8} = 15\text{J}$

2. A satellite is revolving in a stable circular orbit of radius  $R$  and time period is  $T$ . If orbital radius of an another satellite is  $1.03 R$ , then the percentage change in time period of the second satellite as compared to the first will be :

(1) 1.5%                      (2) 4.5%                      (3) 7.5%                      (4) 9%

**Ans. (2)**

**Sol.**  $T^2 \propto r^3$

$$T \propto r^{3/2}$$

$$\frac{dT}{T} = \frac{3}{2} \frac{dr}{r} = \frac{3}{2} \times 3\% = 4.5\%$$

3. In a parallel plate capacitor, the length, width and separation between the plates are respectively  $l = 5$  cm,  $b = 3$  cm and  $d = 1 \mu\text{m}$ . What will be the dimensions of an another capacitor, so that its capacitance becomes 10 times

(1)  $l = 50$  cm,  $b = 30$  cm,  $d = 10 \mu\text{m}$                       (2)  $l = 50$  cm,  $b = 10$  cm,  $d = 10 \mu\text{m}$   
 (3)  $l = 10$  cm,  $b = 30$  cm,  $d = 50 \mu\text{m}$                       (4)  $l = 40$  cm,  $b = 10$  cm,  $d = 50 \mu\text{m}$

**Ans. (1)**

**Sol.**  $C = \frac{\epsilon_0 A}{d} = \frac{\epsilon_0 (\ell b)}{d}$

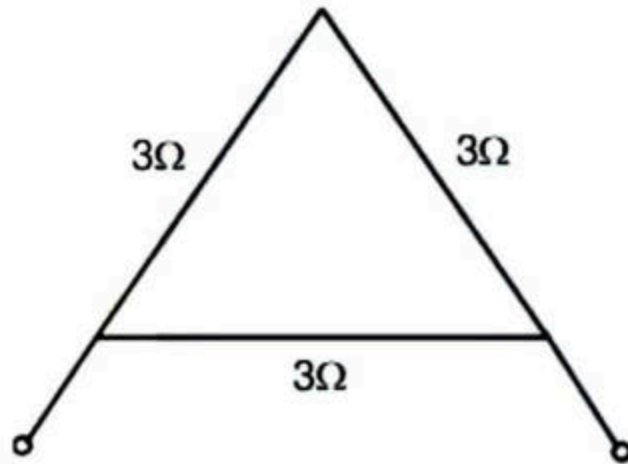
In option (A)  $\ell \rightarrow 10$  times,  $b \rightarrow 10$  times,  $d \rightarrow 10$  so  $C$  will also be 10 times.

4. Resistance of uniform wire is  $9\Omega$ . If it is bent in the form of an equilateral triangle, then equivalent resistance between its two vertices will be :

- (1)  $1\Omega$  (2)  $2\Omega$  (3)  $3\Omega$  (4)  $6\Omega$

**Ans.** (2)

**Sol.**



$$\frac{1}{R_{eq}} = \frac{1}{3} + \frac{1}{6}$$

$$R_{eq} = 2\Omega$$

5. A Solid cylinder of mass  $m$  and radius  $r$  is released from rest at the top of a rough inclined plane making an angle of  $45^\circ$  with the horizontal. Assuming the cylinder rolls without slipping find the acceleration of the axis of the cylinder

- (1)  $\frac{g}{2}$  (2)  $\frac{g}{\sqrt{2}}$  (3)  $\frac{2g}{3\sqrt{2}}$  (4)  $\frac{g}{3\sqrt{2}}$

**Ans.** (3)

**Sol.**  $a = \frac{g \sin \theta}{1 + \frac{K^2}{R^2}}$

$$\frac{K^2}{R^2} = \frac{1}{2}$$

$$\sin 45^\circ = \frac{1}{\sqrt{2}}$$

$$a = \frac{g \times \frac{1}{\sqrt{2}}}{3/2} = \frac{2g}{3\sqrt{2}}$$

6. If  $I = I_A \sin \omega t + I_B \cos \omega t$ , Then find rms value of current.

- (1)  $I_{rms} = I_A + I_B$  (2)  $I_{rms} = \sqrt{I_A^2 + I_B^2}$  (3)  $I_{rms} = \frac{1}{2} \sqrt{I_A^2 + I_B^2}$  (4)  $I_{rms} = \sqrt{\frac{I_A^2 + I_B^2}{2}}$

**Ans.** (4)

**Sol.**  $I_{\max} = \sqrt{I_A^2 + I_B^2}$   
 $I_{\text{rms}} = \sqrt{\frac{I_A^2 + I_B^2}{2}}$

7. Work done by a force  $F = (\alpha + \beta x^2)$  from  $x = 0$  to  $x = 1$  is 5J. If  $\alpha = 1$ , then find value of  $\beta$ .  
 (1) 4 (2) 8 (3) 12 (4) 16

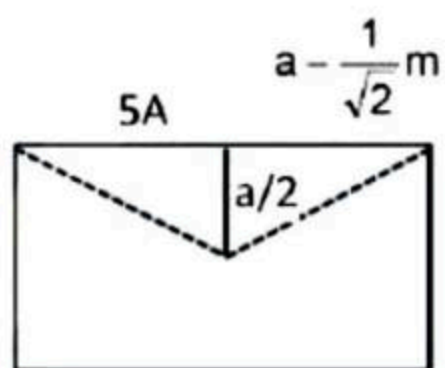
**Ans.** (3)

**Sol.**  $W = \int F dx$

$$5 = \alpha x + \beta \frac{x^3}{3} \Big|_0^1$$

$$5 = 1 \times 1 + \frac{\beta}{3} \times 1 \Rightarrow \beta = 12$$

8. In a square loop of side length  $\frac{1}{\sqrt{2}} \text{ m}$ , current of 5 Amp is flowing. Find magnetic field as its centre (in  $\mu\text{T}$ ).



- (1) 3 (2) 9 (3) 11 (4) 8

**Ans.** (4)

**Sol.**  $B_C = \frac{\mu_0 i}{\pi a} 2\sqrt{2}$

$$= \frac{\mu_0 \times 5}{\pi \frac{1}{\sqrt{2}}} \times 2\sqrt{2}$$

$$= \frac{\mu_0}{\pi} \times 20 = \frac{4\pi \times 10^{-7} \times 10}{\pi}$$

$$80 \times 10^{-7}$$

$$8 \times 10^{-7} = N \times 10^{-7}$$

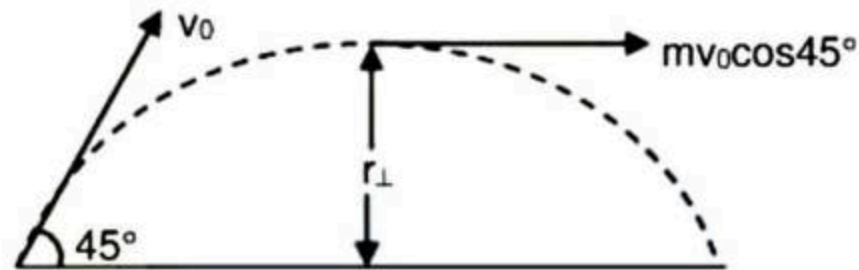
$$N = 8$$

9. A body projected with initial velocity  $V_0$  at  $45^\circ$  angle in X-Y plane. Angular momentum of the particle at highest point about point of projection is :

- (1)  $\frac{mV_0^3}{4g}$  (2)  $\frac{mV_0^3}{4\sqrt{2}g}$  (3)  $\frac{mV_0^2}{4\sqrt{2}g}$  (4)  $\frac{mV_0}{2\sqrt{2}g}$

Ans. (2)

Sol.



$$\vec{L} = \vec{r} \times \vec{p}$$

$$\vec{L} = mv_0 \cos 45^\circ$$

$$L = mvH$$

$$= m \times v_0 \cos 45^\circ \times \frac{u^2 \sin^2 45^\circ}{2g}$$

$$= mv_0 \times \frac{1}{\sqrt{2}} \times \frac{v_0^2}{4g}$$

$$L = \frac{m v_0^3}{4\sqrt{2}g} \Rightarrow \vec{L} = \frac{m v_0^3}{4\sqrt{2}g} (-\hat{k})$$

10. An electron jumps from principle quantum state A to C by releasing photon of wavelength  $2000 \text{ \AA}$  and from state B to C by releasing of photon of wavelength  $6000 \text{ \AA}$ , then find wavelength of photon for transition from A to B.

- (1)  $2000 \text{ \AA}$  (2)  $3000 \text{ \AA}$  (3)  $4000 \text{ \AA}$  (4)  $8000 \text{ \AA}$

Ans. (2)

Sol.  $E_A - E_C = \frac{hc}{2000}$

$$E_B - E_C = \frac{hc}{6000}$$

$$E_A - E_B = \frac{hc}{\lambda}$$

$$E_A - E_B = \frac{hc}{2000} - \frac{hc}{6000} = \frac{hc}{\lambda}$$

$$\Rightarrow \frac{3-1}{6000} = \frac{1}{\lambda}$$

$$\lambda = \frac{6000}{2} = 3000 \text{ \AA}$$

11. Initial velocity of an electron is  $v_0 \hat{i}$  and its initial De-Broglie wavelength is  $\lambda_0$ . A uniform electric field of  $\vec{E} = -E_0 \hat{k}$  is applied. The De-Broglie wavelength as a function of time will be :-

(1)  $\lambda(t) = \lambda_0$

(2)  $\lambda(t) = \frac{h}{\sqrt{\left(\frac{1}{\lambda_0}\right)^2 + \left(\frac{eE_0 t}{h}\right)^2}}$

(3)  $\lambda(t) = \frac{1}{\sqrt{\left(\frac{1}{\lambda_0}\right)^2 + \left(\frac{eE_0 t}{h}\right)^2}}$

(4)  $\lambda(t) = \frac{1}{\sqrt{\left(\frac{1}{\lambda_0}\right)^2 + \left(\frac{eE_0 t}{mh}\right)^2}}$

Ans. (3)

Sol.  $\lambda_0 = \frac{h}{mv_0} \Rightarrow mv_0 = \frac{h}{\lambda_0}$

$$\vec{V} = \vec{u} + \vec{a}t \Rightarrow \dot{V}(t) = v_0 \hat{i} + \frac{(-e)(-E_0 \hat{k})}{m} t$$

$$\dot{V} = v_0 \hat{i} + \frac{eE_0}{m} t \hat{k} \Rightarrow |\dot{V}| = \sqrt{v_0^2 + \left(\frac{eE_0}{m} t\right)^2}$$

$$\lambda_{ab}(t) = \frac{h}{m|\dot{V}|} = \frac{h}{m\sqrt{v_0^2 + \left(\frac{eE_0}{m} t\right)^2}} = \frac{h}{\sqrt{\left(\frac{h}{\lambda_0}\right)^2 + \left(\frac{eE_0}{m} t\right)^2}}$$

$$\lambda_{ab}(t) = \frac{1}{\sqrt{\left(\frac{1}{\lambda_0}\right)^2 + \left(\frac{eE_0 t}{h}\right)^2}}$$

12. Radius of curvature of a plano convex lens is 2 cm and refractive index is 1.5 has focal length  $f_1$  in air and  $f_2$  in a medium of refractive index 1.2, calculate  $f_1 / f_2$

(1) 2 : 1

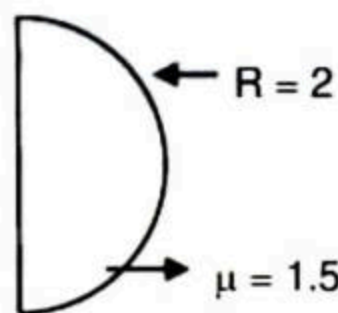
(2) 1 : 2

(3) 3 : 2

(4) 1 : 4

Ans. (2)

Sol.



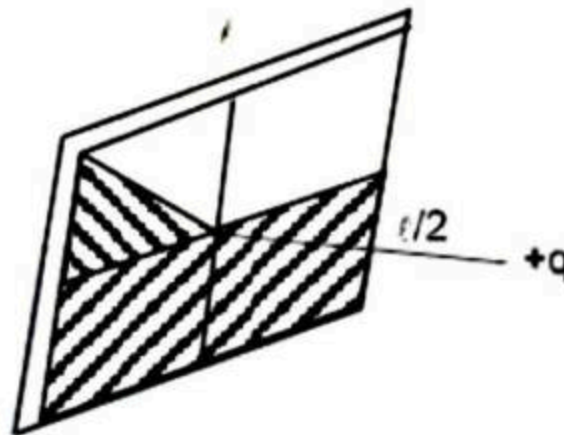
$$\frac{1}{f_1} = (1.5 - 1) \times \frac{1}{2} = \frac{1}{4} \Rightarrow f_1 = 4$$

$$\frac{1}{f_2} = \left(\frac{1.5}{1.2} - 1\right) \times \frac{1}{2} = \frac{0.3}{2 \times 1.2} = \frac{1}{8}$$

$$f_2 = 8$$

$$\frac{f_1}{f_2} = \frac{4}{8} = \frac{1}{2}$$

13. A point charge  $+1\text{C}$  is placed at a distance  $\frac{\ell}{2}$  from center of a square surface of side length  $\ell$ . If the flux passing through the shaded region is then  $\phi = \frac{5}{x\epsilon_0}$ , then write the value of  $x$



**Ans.** 48.00

**Sol.** flux passing through the complete square surface  $= \frac{q}{6\epsilon_0}$

8 triangular surface .....  $\phi = \frac{5}{6\epsilon_0}$

1 triangular surface .....  $\frac{q}{48\epsilon_0}$

5 triangular surface .....  $\phi = \frac{q}{48\epsilon_0} \times 5$

$$\phi = \frac{5q}{48\epsilon_0} \text{ where } q = 1\text{C} = \frac{5}{48\epsilon_0} = \frac{5}{x\epsilon_0}$$

$x = 48$

14. Find minimum order of maxima of wavelength  $\lambda_1$  on screen in YDSE where maxima of  $\lambda_1 = 480\text{ nm}$  coincide with maxima of  $\lambda_2 = 600\text{ nm}$ .

(1) 5

(2) 4

(3) 3

(4) 1

**Ans.** (1)

**Sol.**  $\lambda_1 = 480\text{ nm}$

$\lambda_2 = 600\text{ nm}$

$n_1 = ?$

$y = n_1\lambda_1 = n_2\lambda_2$

$$\Rightarrow \frac{n_1}{n_2} = \frac{600}{480} = \frac{5}{4}$$

$n_1 = 5$

15. In a process pressure of the gas is directly proportional to temperature then choose correct option  
 (A) Process is isochoric  
 (B) Work done in process is zero  
 (C) Internal energy increases with increase in temperature  
 (1) A and B are correct (2) A and C are correct  
 (3) A, B and C are correct (4) B and C are correct

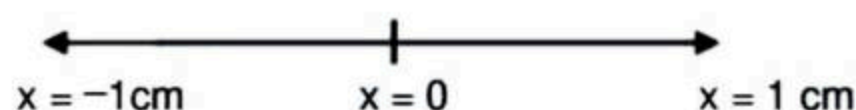
Ans. (3)

Sol.  $P \propto T$  (volume is constant)  
 process is isochoric  
 $\text{work} = P\Delta V = 0$   
 $\Delta U = nC_v\Delta T$   
 $\Delta U$  increase if temperature increase

16. A particle executes SHM with its time period 2 second and has amplitude of 1 cm. What is the ratio of total distance and displacement in 12.5 second :  
 (1) 25 : 1 (2) 5 : 1 (3) 4 : 5 (4) 3 : 2

Ans. (1)

Sol.



12 second + 0.5 second

$$\text{Distance} = \frac{4}{2} \times 12 + \frac{4}{2} \times 0.5$$

$$= 24 + 1 = 25 \text{ cm}$$

Displacement = 1 cm

$$\frac{\text{Distance}}{\text{Displacement}} = \frac{25}{1}$$

17. Find the maximum possible velocity for the given angle of banking  $\theta$  on a curved road of radius of curvature  $r$  having coefficient of friction  $\mu$ .

(1)  $v_{\max} = \sqrt{\frac{gr(\mu + \tan \theta)}{(1 - \mu \tan \theta)}}$

(2)  $v_{\max} = \sqrt{\frac{gr(\mu - \tan \theta)}{(1 - \mu \tan \theta)}}$

(3)  $v_{\max} = \sqrt{\frac{gr(1 + \tan \theta)}{(1 - \mu \tan \theta)}}$

(4)  $v_{\max} = \sqrt{\frac{gr(\mu - \tan \theta)}{(1 + \mu \tan \theta)}}$

Ans. (1)

18. What is the fractional decrease in focal length of a lens when optical power is increased from 2.5 D to 2.6 D.  
 (1) 0.05 (2) 0.04 (3) 0.10 (4) 0.25

Ans. (2)

Sol.  $f = \frac{1}{P}$

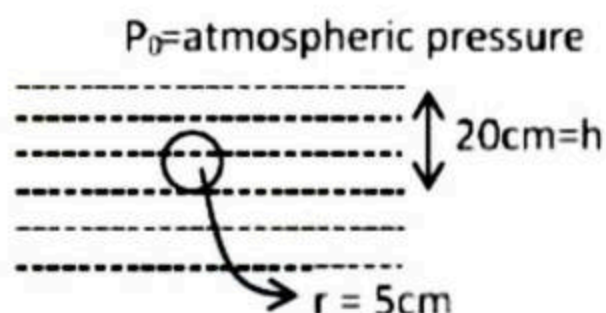
$$\frac{\Delta f}{f} = \frac{\Delta P}{P} = \frac{2.6 - 2.5}{2.5} = \frac{1}{25} = 0.04$$

19. A water bubble is at a depth of 20 cm and radius of bubble is 1 cm. If the inner pressure of the bubble is greater than the atmospheric pressure by 2100 N/m<sup>2</sup> then find the surface tension?

(1) 0.6 (2) 0.5 (3) 0.8 (4) 0.4

Ans. (2)

Sol.



$$P_{\text{in}} - P_0 = 2100 \quad \dots (i)$$

$$P_{\text{in}} - P_0 = \frac{2T}{R} + h\rho g \quad \dots (ii)$$

From (i) and (ii)

$$2100 = \rho gh + \frac{2T}{R}$$

$$\frac{2T}{R} = 2100 - \rho gh$$

$$T = 0.5$$

20. If the distance between two parallel plates of a capacitor is  $d$ ,  $A$  is the area of each plate, and  $E$  is the electric field between both the plates. Find the energy stored in capacitor.

(1)  $\frac{1}{2} E^2 A \epsilon_0 d$  (2)  $\frac{1}{4} E^2 A \epsilon_0 d$  (3)  $\frac{3}{4} E^2 A \epsilon_0 d$  (4)  $E^2 A \epsilon_0 d$

Ans. (1)

Sol. Energy density ( $u$ ) =  $\frac{1}{2} \epsilon_0 E^2$

Energy stored = energy density  $\times$  volume

$$= \frac{1}{2} \epsilon_0 E^2 \times (A \times d)$$

$$= \frac{1}{2} E^2 A \epsilon_0 d$$

## PART : CHEMISTRY

1. Difference of B.P and M.P in oxygen and sulphur can be explained by  
 (1) Atomicity (2) Atomic mass (3) Electronegativity (4) Electron gain enthalphy

**Ans. (1)**

**Sol.** The large difference between the melting and boiling points of oxygen and sulphur may be explained on the basis of their atomicity.  $O_2$  exist as diatomic molecule where sulphur exist as polyatomic molecule  $S_8$

2. Which of the following strong oxidising agent?  
 (1)  $Eu^{+2}$  (2)  $Ce^{2+}$  (3)  $Ce^{4+}$  (4)  $Eu^{4+}$

**Ans. (4)**

**Sol.**  $M^{4+}$  will reduce itself to stable (+3) so, it will be good Oxidizing agent.

3. If 280 kg CO and 2320 kg of  $Fe_3O_4$  are made to react according to



what is the weight of Fe produce (in kg)

Given : Mol. Wt. of CO and  $Fe_3O_4$  are 28 and 232 u

**Ans. (420)**

**Sol.**

|                      |   |       |   |                        |
|----------------------|---|-------|---|------------------------|
| $Fe_3O_4$            | + | 4 CO  | → | 3Fe + 4CO <sub>2</sub> |
| n <sub>i</sub> 10000 |   | 10000 |   |                        |
|                      |   | (LR)  |   |                        |

$$n_f \quad \quad \quad 10000 \times \frac{3}{4} = 7500$$

$$\therefore W_{Fe} = 7500 \times 56 \text{ g} = 420 \text{ kg}$$

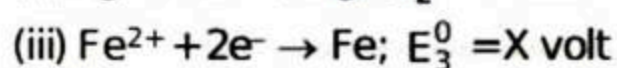
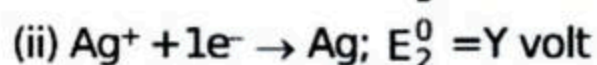
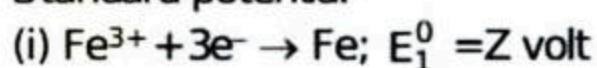
4. A reaction is non spontaneous at freezing point and spontaneous at boiling point select the correct option

- (1) Both  $\Delta H$  and  $\Delta S$  are positive (2)  $\Delta H > 0, \Delta S < 0$   
 (3)  $\Delta H < 0, \Delta S > 0$  (4) Both  $\Delta H$  and  $\Delta S$  are negative

**Ans. (1)**

|                            |                            |
|----------------------------|----------------------------|
| <b>Sol. Case I</b>         | <b>Case II</b>             |
| At freezing point          | At boiling point           |
| $\Delta G > 0$             | $\Delta G < 0$             |
| $\Delta G - T\Delta S > 0$ | $\Delta H - T\Delta S < 0$ |
| $ \Delta G  >  T\Delta S $ | $ \Delta H  <  T\Delta S $ |

5. Standard potential



Find  $E^0$  of reaction  $Fe^{2+} + Ag^+ \rightarrow Fe^{3+} + Ag(s)$

- (1)  $(Z - 2X + 3Y)$  volt (2)  $(X - 2Y + 3Z)$  volt (3)  $(Y - 2Z + 3X)$  volt (4)  $(Y - 3Z + 2X)$  volt

**Ans. (4)**

**Sol.**  $Fe^{3+} + e^- \rightarrow Fe^{2+}$

(iv) = (i) - (iii)

$$\Delta G_4^0 = \Delta G_1^0 - \Delta G_3^0$$

$$-1.f.E_4^0 = -3.f.E_1^0 + 2.f.E_3^0$$

$$E_4^0 = 3E_1^0 - 2E_3^0 = 3Z - 2X$$

$$E^0 = E_{\frac{Ag^+}{Ag}}^0 - E_{\frac{Fe^{2+}}{Fe^{3+}}}^0 = Y - E_{\frac{Fe^{2+}}{Fe^{3+}}}^0 = Y - 3Z + 2X$$

6. In a process pressure of gas is directly proportional to temperature then choose correct option  
 (A) Process is isochoric  
 (B) Work done in process is zero  
 (C) Internal energy increases with increase in temperature  
 (1) A and B are correct (2) A and C are correct  
 (3) A, B and C are correct (4) B and C are correct

**Ans. (3)**

**Sol.**  $P \propto T$  ( $V, n = \text{constant}$ )

7. 1 mole of a complex with molecular formula  $\text{Co}(\text{NH}_3)_5\text{Cl}_3$  produces 3 mole ions upon complete ionisation. Upon adding excess  $\text{AgNO}_3$ , 2 mole  $\text{AgCl}$  are precipitated. Complex is:  
 (1)  $[\text{Co}(\text{NH}_3)_5\text{Cl}]\text{Cl}_2$  (2)  $[\text{Co}(\text{NH}_3)_4\text{Cl}_2]\text{Cl} \cdot \text{NH}_3$   
 (3)  $[\text{Co}(\text{NH}_3)_3\text{Cl}_3] \cdot 2\text{NH}_3$  (4)  $[\text{Co}(\text{NH}_3)_4\text{Cl}]\text{Cl}_2 \cdot \text{NH}_3$

**Ans. (1)**

**Sol.**  $2\text{Cl}^-$  should be outside square bracket. Also,  $\text{Co}^{3+}$  shows CN = 6

$\therefore$  Complex :  $[\text{Co}(\text{NH}_3)_5\text{Cl}]\text{Cl}_2$

8. Consider  $\text{H}_2\text{O}$ ,  $\text{NH}_3$ ,  $\text{CH}_4$  and select correct statements:  
 (A) All are  $\text{sp}^3$  hybridised  
 (B) Bond angle  $\text{H}-\text{O}-\text{H}$ ,  $\text{H}-\text{N}-\text{H}$ ,  $\text{H}-\text{C}-\text{H}$  are  $104.5^\circ$ ,  $107^\circ$ ,  $109.5^\circ$   
 (C) Dipole moment:  $\text{CH}_4 < \text{NH}_3 < \text{H}_2\text{O}$   
 (D)  $\text{H}_2\text{O}$  and  $\text{NH}_3$  are lewis base and lewis acid  
 (E)  $\text{NH}_3$  in  $\text{H}_2\text{O}$  is basic in nature

(1) A, B, C and E (2) A, B and D (3) A, C, D (4) B, D, E

**Ans. (1)**

**Sol.** Both  $\text{NH}_3$  and  $\text{H}_2\text{O}$  behave as lewis base.

9. Which of the following is not true combination from given statement.  
 (a) Elements in periodic table are linearly arranged with atomic weight  
 (b) Elements in periodic table are linearly arranged with atomic number  
 (c) Element having similar electronic configuration are arranged in same group  
 (d) Using periodic table we can identify in which subshell last electron enters  
 (e) Isotopes of an element are placed in periodic table.

(1) a, e only (2) b, e only (3) b, c, d only (4) a, c, d, e only

**Ans. (1)**

10. If the  $K_{sp}$  of  $\text{Cr}(\text{OH})_3$  is  $1.6 \times 10^{-30} \text{ M}^4$  the molar solubility of salt in water is

(1)  $\left(\frac{1.6 \times 10^{-30}}{27}\right)^{1/4}$  (2)  $\left(\frac{16}{27} \times 10^{-30}\right)^{1/4}$  (3)  $\left(\frac{160}{27} \times 10^{-30}\right)^{1/4}$  (4) None of these

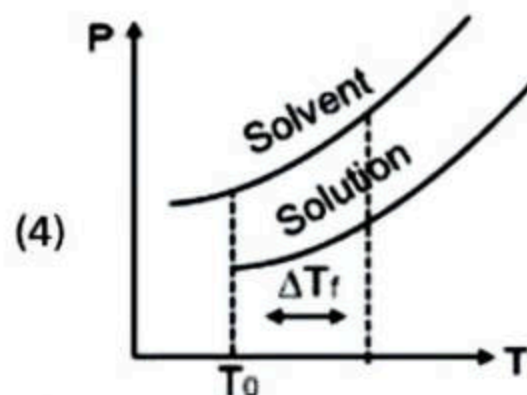
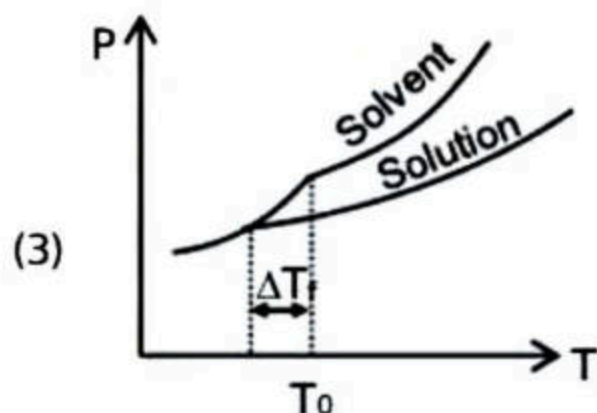
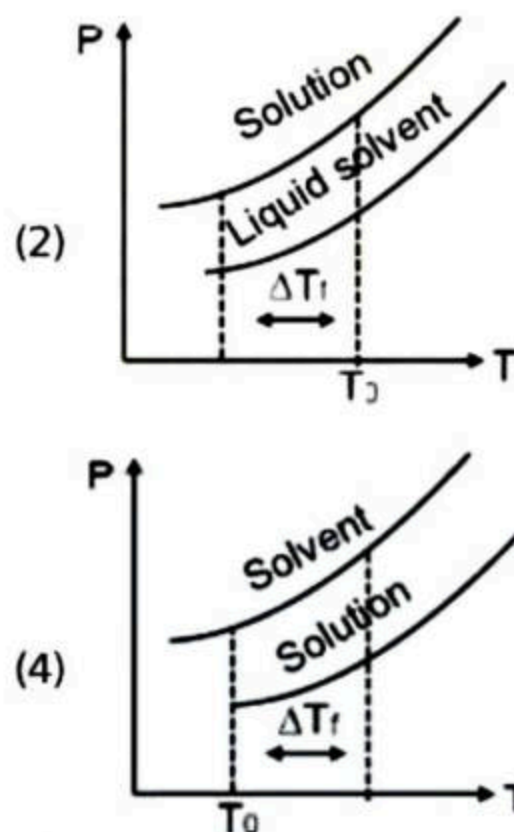
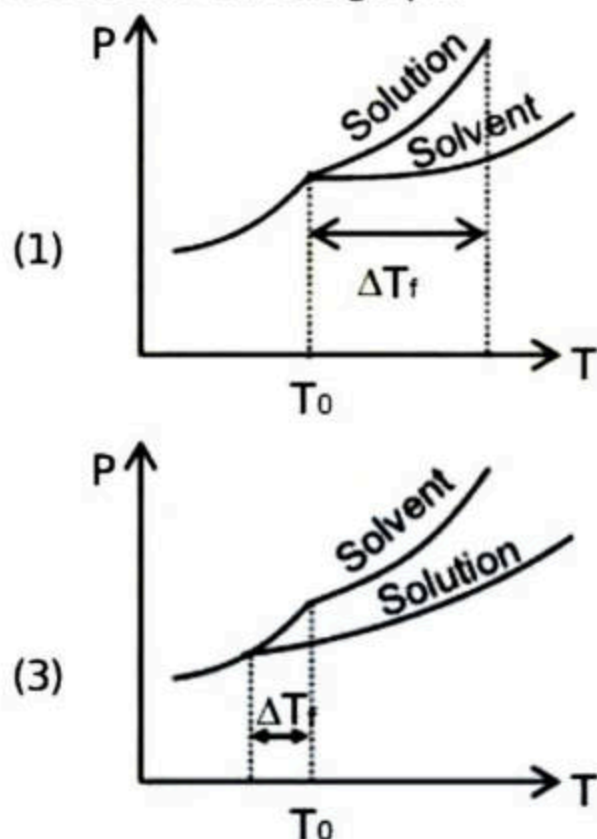
**Ans. (1)**

**Sol.**  $\text{Cr}(\text{OH})_3(s) \rightleftharpoons \underset{s}{\text{Cr}^{3+}} + \underset{3s}{3\text{OH}^-}$

$$K_{sp} = [\text{Cr}^{3+}][\text{OH}^-]^3 = s(3s)^3 = 27s^4$$

$$s = \left(\frac{1.6 \times 10^{-30}}{27}\right)^{1/4}$$

11. Select the correct graph.



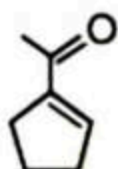
Ans.

(3)

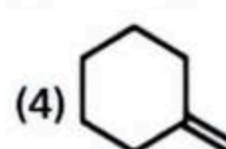
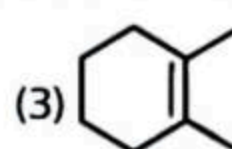
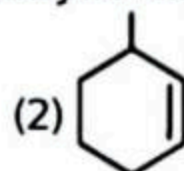
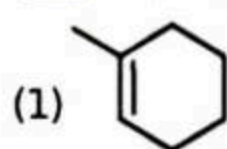
Sol.

T at which  $VP_{\text{solid}} = VP_{\text{liquid}}$  is freezing point of solution is less than that of solvent.

12.



is formed by ozonolysis followed by aldol condensation of Alkene. Alkene can be:



Ans.

(1)

13.

Ribose present in DNA

(A) It is a pentose sugar

(B) It is present in pyranose form

(C) It is present in D-configuration

(D) It is reducing sugar in free form

(E)  $\alpha$  anomeric form is present.

Correct options are :

(1) A, C, D

(2) A, B, D

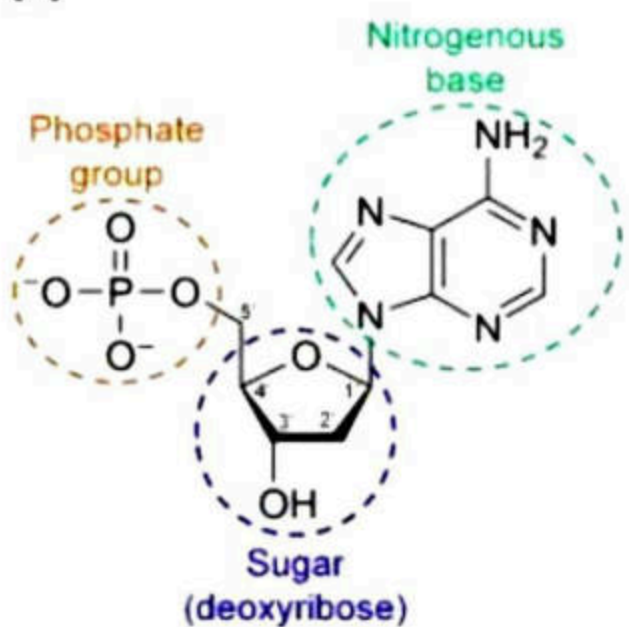
(3) A, B, C, D, E

(4) A, C, E

Ans.

(1)

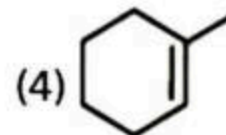
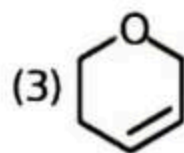
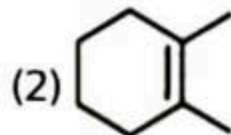
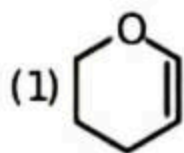
Sol.



14. Arrange following for reaction rate with nucleophilic attack  
 (a) Acetophenone (b) p-tolylaldehyde  
 (c) Benzaldehyde (d) p-Nitrobenzaldehyde  
 (1)  $d > c > b > a$  (2)  $a > c > b > d$  (3)  $d > b > c > a$  (4)  $d > a > b > c$

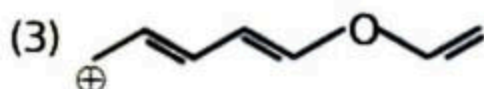
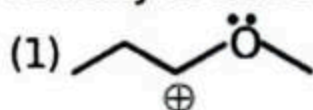
Ans. (1)

15. Which compound react fastest with HBr?



Ans. (1)

16. Stability of carbocation is maximum is?

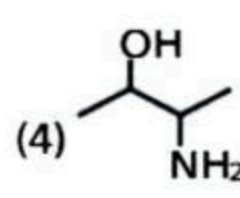
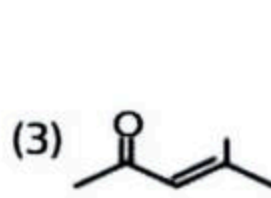
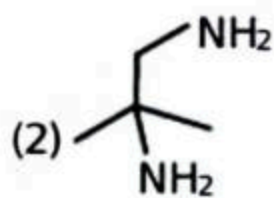
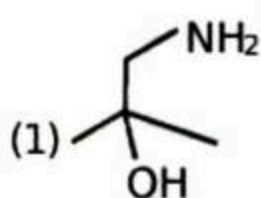


Ans. (2)

17. **Statement-I** : Dumas method is used for estimation of Nitrogen.  
**Statement-II** : In Dumas method Nitrogen present in compound is converted to  $(\text{NH}_4)_2\text{SO}_4$   
 (1) Both Statement I and statement II are true  
 (2) Both statement I and statement II are false  
 (3) Statement I is true but statement II is false  
 (4) Statement I is false but statement II is true

Ans. (3)

18.  $\text{CH}_3\text{C}\equiv\text{CH} \xrightarrow[3. \text{H}_2/\text{Ni}]{1. \text{HgSO}_4, 2. \text{HCN}/\text{HO}^\ominus}$



Ans. (1)

19. **Statement-I** :  $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{Cl} + \text{OH}^\ominus \longrightarrow$  Reaction is favoured in less polar solvent.  
**Statement-II** :  $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{Cl} + \text{R}_3\text{N} \longrightarrow$  Reaction is favoured in more polar solvent.  
 (1) Both Statement I and statement II are true (2) Both statement I and statement II are false  
 (3) Statement I is true but statement II is false (4) Statement I is false but statement II is true

Ans. (1)

## PART : MATHEMATICS

1. Evaluate :

$$\lim_{x \rightarrow 0} \operatorname{cosec} x \left( \sqrt{2\cos^2 x + 3\cos x} - \sqrt{\cos^2 x + \sin x + 4} \right)$$

- (1) 0                      (2) 1                      (3)  $\frac{1}{2\sqrt{5}}$                       (4)  $-\frac{1}{2\sqrt{5}}$

Ans. (4)

Sol. 
$$= \lim_{x \rightarrow 0} \frac{1}{\sin x} \frac{(2\cos^2 x + 3\cos x - \cos^2 x - \sin x - 4)}{\sqrt{2\cos^2 x + 3\cos x} + \sqrt{\cos^2 x + \sin x + 4}}$$

$$= \frac{1}{2\sqrt{5}} \lim_{x \rightarrow 0} \frac{(\cos^2 x + 3\cos x - \sin x - 4)}{\sin x} \quad \left( \frac{0}{0} \right)$$

By L' Hospital Rule

$$= \frac{1}{2\sqrt{5}} \lim_{x \rightarrow 0} \frac{2\cos x(-\sin x) - 3\sin x - \cos x}{\cos x}$$

$$= -\frac{1}{2\sqrt{5}}$$

2. Two students A & B throw two dices one by one. A wins the game when sum of numbers is 5 and B wins when the sum of numbers is 8. If A start the game then find probability that A wins the game

- (1)  $\frac{11}{19}$                       (2)  $\frac{12}{19}$                       (3)  $\frac{9}{19}$                       (4)  $\frac{10}{19}$

Ans. (3)

Sol.  $P(\text{sum } 5) = \frac{4}{36}$

$$P(\text{sum } 8) = \frac{5}{36}$$

$$P(\text{A wins the game}) = P(A) + P(\bar{A}B\bar{A}) + P(\bar{A}\bar{B}\bar{A}B\bar{A}) + \dots \infty$$

$$= \frac{4}{36} + \left( \frac{32}{36} \right) \left( \frac{31}{36} \right) \left( \frac{4}{36} \right) + \dots \infty$$

$$= \frac{\frac{4}{36}}{1 - \left( \frac{32}{36} \right) \left( \frac{31}{36} \right)}$$

$$= \frac{4}{36} \times \frac{36^2}{(1296 - 992)}$$

$$= \frac{144}{304} = \frac{36}{76} = \frac{9}{19}$$

3. If the 5<sup>th</sup>, 6<sup>th</sup> and 7<sup>th</sup> term of the binomial expansion of  $(1+x^2)^{n+4}$  are in A.P. Then greatest binomial coefficient in the expansion of  $(1+x^2)^{n+4}$  is:

(1)  ${}^{16}C_8$  (2)  ${}^{14}C_7$  (3)  ${}^{12}C_6$  (4)  ${}^{13}C_7$

Ans. (2)

Sol.  ${}^{n+4}C_4, {}^{n+4}C_5, {}^{n+4}C_6$  are in A.P.

$$2 {}^{n+4}C_5 = {}^{n+4}C_4 + {}^{n+4}C_6$$

$$\frac{2 \frac{n+4}{n-1} \frac{n+4}{5} = \frac{n+4}{n} \frac{n+4}{4} + \frac{n+4}{n-2} \frac{n+4}{6}}$$

$$2(6)n = (6)(5) + n(n-1)$$

$$12n = 30 + n^2 - n$$

$$n^2 - 13n + 30 = 0$$

$$(n-3)(n-10) = 0$$

$$n = 3, 10$$

But  $n = 3$  is not possible.

Now in expansion of  $(1+x^2)^{14}$ , greatest binomial coefficient =  ${}^{14}C_7$

4. If A is  $3 \times 3$  order matrix, such that  $|A| = 2$  then value of  $|\text{adj}(\text{adj}(\text{adj}(\text{adj} A)))|$  is equal to

(1)  $2^{32}$  (2)  $2^{16}$  (3)  $2^{20}$  (4)  $2^8$

Ans. (2)

Sol.  $|A| = 2$

$$|\text{adj}(\text{adj}(\text{adj}(\text{adj} A)))|$$

$$|\text{adj}(\text{adj}(\text{adj} A))|^2$$

$$|\text{adj}(\text{adj} A)|^4$$

$$|\text{adj} A|^8$$

$$|A|^{16}$$

$$2^{16}$$

5. Let  $S_n = \frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \dots$ , If  $\sqrt{2026 \times S_{2025}}$  = sum of 6 terms of an A.P. whose first term is  $-p$  and common difference is  $p$  then find difference of 20<sup>th</sup> term and 15<sup>th</sup> term of that A.P.

Ans. (25)

Sol.  $T_n$  of  $\frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \dots$  is  $\frac{1}{n^2 + n} = \frac{1}{n(n+1)}$

$$S_{2025} = \sum_{n=1}^{2025} \left( \frac{1}{n} - \frac{1}{n+1} \right)$$

$$= \left( \frac{1}{1} - \frac{1}{2} \right) + \left( \frac{1}{2} - \frac{1}{3} \right) + \dots + \left( \frac{1}{2025} - \frac{1}{2026} \right)$$

$$= 1 - \frac{1}{2026} = \frac{2025}{2026}$$

Now,

$$\sqrt{2026 \times \frac{2025}{2026}} = \frac{6}{2} [-2p + (6-1)p]$$

$$45 = 3(3p) \quad p = 5$$

Now,

$$A_{20} - A_{15} = [-5 + (19)(5)] - [-5 + (14)(5)] \\ = 95 - 70 = 25$$

6. If  $(x+2)^2 f(x) + 3(x+2)^2 = \int_0^x (t+2)f(t)dt$  then  $f(2) = ?$

(1)  $\frac{9}{2}$

(2)  $-\frac{9}{2}$

(3)  $\frac{7}{2}$

(4)  $-\frac{7}{2}$

Ans. (2)

Sol.  $(x+2)^2 f(x) + 3(x+2)^2 = \int_0^x ((t+2)f(t))dt$

$$2(x+2)f(x) + (x+2)^2 f'(x) + 6(x+2) = (x+2)f(x)$$

$$2f(x) + (x+2)f'(x) + 6 = f(x)$$

$$(x+2)f'(x) = -f(x) - 6$$

$$(x+2) \frac{dy}{dx} = -y - 6$$

$$\frac{dy}{y+6} = -\int \frac{dx}{x+2}$$

$$\ln(y+6) = -\ln(x+2) + c \quad (1)$$

$$(x+2)^2 f(x) + 3(x+2)^2 = \int_0^x (t+2)f(t)dt$$

put  $x = 0$

$$4f(0) + 12 = 0$$

$$f(0) = -3 \quad (2)$$

put  $x = 0$  is equation (1)

$$\ln 3 = -\ln 2 + c$$

$$c = \ln 6$$

$$\ln(y+6) = -\ln(x+2) + \ln 6$$

$$(y+6) = \frac{6}{(x+2)}$$

then  $x = 2$

$$y+6 = \frac{6}{4}$$

$$y = \frac{3}{2} - 6$$

$$y = -\frac{9}{2}$$

so  $f(2) = -\frac{9}{2}$

7. If  $\alpha$  and  $\beta$  are real numbers such that  $\sec^2(\tan^{-1}(\alpha)) + \operatorname{cosec}^2(\cot^{-1}(\beta)) = 36$  and  $\alpha + \beta = 8$ , ( $\alpha > \beta$ ) then  $\alpha^3 + \beta^3$  is:

(1) 150 (2) 152 (3) 148 (4) 146

Ans. (2)

Sol.  $1 + \tan^2(\tan^{-1}\alpha) + 1 + \cot^2(\cot^{-1}\beta) = 36$

$$2 + \alpha^2 + \beta^2 = 36$$

$$\alpha^2 + \beta^2 = 34$$

$$(\alpha + \beta)^2 - 2\alpha\beta = 34$$

$$8^2 - 2\alpha\beta = 34 \Rightarrow 2\alpha\beta = 30 \Rightarrow \alpha\beta = 15$$

$$\text{So, } \alpha + \beta = 8 \text{ and } \alpha\beta = 15$$

$$\alpha = 5 \text{ and } \beta = 3$$

$$\alpha^3 + \beta^3 = 125 + 27 = 152$$

8. Let  $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$ ,  $\vec{b} = 3\hat{i} + \hat{j} - \hat{k}$ ,  $\vec{c}$  is a vector perpendicular to  $\vec{b}$ , also  $\vec{c}$  is coplanar with  $\vec{a}$  and  $\vec{b}$ . If  $\vec{c} \cdot \vec{a} = 5$  then  $|\vec{c}|$  is equal to

(1)  $\sqrt{\frac{13}{6}}$  (2)  $\sqrt{\frac{11}{6}}$  (3)  $\sqrt{\frac{5}{6}}$  (4)  $\sqrt{\frac{7}{6}}$

Ans. (2)

Sol. Let  $\vec{c} = \lambda \vec{b} \times (\vec{a} \times \vec{b})$

$$= \lambda [(\vec{b} \cdot \vec{b})\vec{a} - (\vec{b} \cdot \vec{a})\vec{b}]$$

$$= \lambda [11\vec{a} - 2\vec{b}]$$

$$= \lambda [11\hat{i} + 22\hat{j} + 33\hat{k} - 6\hat{i} - 2\hat{j} + 2\hat{k}]$$

$$= \lambda [5\hat{i} + 20\hat{j} + 35\hat{k}]$$

$$\vec{c} = 5\lambda [\hat{i} + 4\hat{j} + 7\hat{k}]$$

Now,  $\vec{c} \cdot \vec{a} = 5$

$$5\lambda [1 + 8 + 21] = 5$$

$$\lambda = \frac{1}{30}$$

$$\vec{c} = \frac{1}{6} (\hat{i} + 4\hat{j} + 7\hat{k})$$

$$|\vec{c}| = \frac{1}{6} \sqrt{1 + 16 + 49}$$

$$|\vec{c}| = \frac{\sqrt{66}}{6} = \sqrt{\frac{11}{6}}$$

9. If system of equations

$$2x - y + z = 4,$$

$$4x - \lambda y + 3z = 12 \text{ and}$$

$$100x - 41y + \mu z = 212 \text{ has infinite solutions then } \mu - 2\lambda \text{ is}$$

(1) 59 (2) 55 (3) 56 (4) 57

**Ans. (2)**

**Sol.** Let equations are  $P_1$ ,  $P_2$  and  $P_3$

Then

$$KP_1 + P_2 : x(2K + 4) + y(-K - \lambda) + z(K + 3) = 4K + 12$$

$$P_3 : 100x - 41y + \mu z = 212$$

Now comparing coefficient

$$\frac{2K + 4}{100} = \frac{-K - \lambda}{-41} = \frac{K + 3}{\mu} = \frac{4K + 12}{212}$$

$$\text{Solving } \frac{2K + 4}{100} = \frac{4K + 12}{212}$$

$$\frac{K + 2}{50} = \frac{K + 3}{53}$$

$$53K + 106 = 50K + 150$$

$$3K = 44$$

$$K = \frac{44}{3}$$

Now

$$\frac{\frac{88}{3} + 4}{100} = \frac{\frac{-44}{3} - \lambda}{-41} = \frac{\frac{44}{3} + 3}{\mu} = \frac{\frac{176}{3} + 12}{212}$$

$$\frac{1}{3} = \frac{44 + 3\lambda}{123} \text{ and } \frac{53}{3\mu} = \frac{212}{3 \times 212} = \mu = 53$$

$$41 = 44 + 3\lambda$$

$$\lambda = -1$$

$$\text{Now } \mu - 2\lambda = 53 - 2(-1) = 55$$

**10.** Find the product of all rational roots of the equation  $(x^2 - 9x + 11)^2 - (x - 4)(x - 5) = 3$ .

**Ans. (14)**

**Sol.**  $(x^2 - 9x + 11)^2 - (x^2 - 9x + 23) = 0$

$$\text{Let } x^2 - 9x + 11 = t.$$

$$t^2 - (t + 12) = 0 \quad \Rightarrow \quad (t - 4)(t + 3) = 0$$

$$t = 4$$

$$x^2 - 9x + 11 = 4$$

$$x^2 - 9x + 7 = 0$$

$$D = 81 - 28 = 53$$

D is not a perfect square  $\Rightarrow$  Irrational value of x.

$$t = -3$$

$$x^2 - 9x + 11 = -3$$

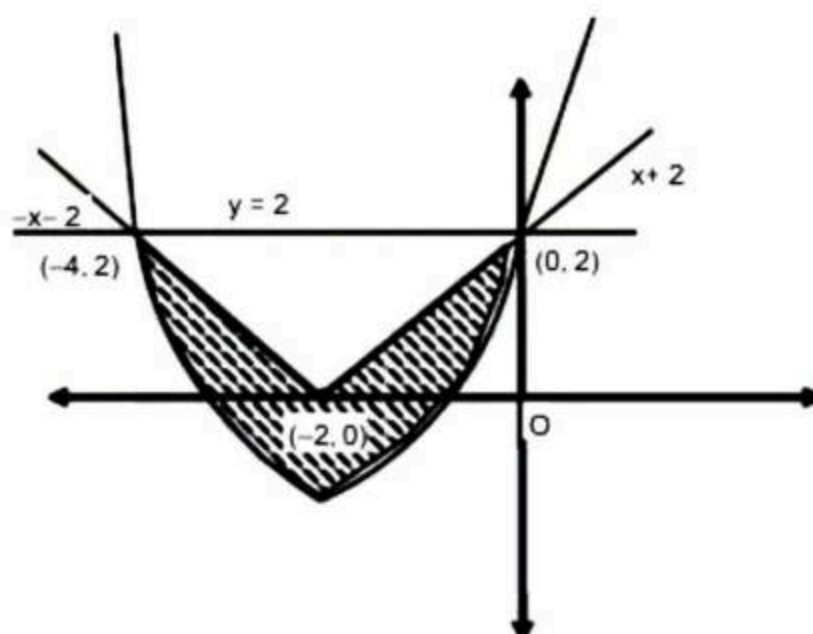
$$x^2 - 9x + 14 = 0$$

$$(x - 7)(x - 2) = 0$$

$$\text{Product of roots} = 7 \times 2 = 14.$$

11. The area of the region bounded by  $S(x, y)$  such that  $S = \{(x, y) : x^2 + 4x + 2 \leq y \leq |x + 2|\}$  is (in sq. units)
- (1)  $\frac{24}{5}$  (2) 5 (3)  $\frac{20}{3}$  (4) 7

**Ans.** (3)  
**Sol.**



$$\begin{aligned}
 \text{Area of shaded region} &= \int_{-4}^0 2 - (x^2 + 4x + 2) dx - \frac{1}{2} \times 4 \times 2 \\
 &= \int_{-4}^0 (-x^2 - 4x) dx - 4 \\
 &= -\int_{-4}^0 (x^2 + 4x) dx - 4 \\
 &= -\left[\frac{x^3}{3} + 2x^2\right]_{-4}^0 - 4 \\
 &= -\left[0 - \left(\frac{-64}{3}\right) - 32\right] - 4 \\
 &= 32 - \frac{64}{3} - 4 \\
 &= 28 - \frac{64}{3} \\
 &= \frac{84 - 64}{3} \\
 &= \frac{20}{3} \text{ sq. units}
 \end{aligned}$$

12. Find number of three digits numbers which are divisible by 2 & 3 both but not by 4 and 9.

**Ans.** (125)

**Sol.** Required numbers are which are divisible by 6

102, 114, 120, 132, 138, 150, 156, 168, .....996 (A.P.) (Total numbers are 150)

Now

Numbers which are divisible by 36

108, 120, 138, .....972 (A.P.) (Total numbers are 25)

Therefore, the required three digit numbers which are divisible by 6 and not by 36 are  $150 - 25 = 125$ .

13. If  $I(m, n) = \int_0^1 x^{m-1}(1-x)^{n-1} dx$ , then  $I(9,14) + I(10,13)$  is equal to

- (1)  $I(7, 11)$  (2)  $I(9, 13)$  (3)  $I(11, 15)$  (4)  $I(8, 11)$

Ans. (2)

Sol. Let  $x = \sin^2 \theta \Rightarrow dx = 2 \sin \theta \cos \theta d\theta$

$$\therefore I(m, n) = \int_0^{\frac{\pi}{2}} \sin^{2m-2} \theta \cos^{2n-2} \theta \cdot 2 \sin \theta \cos \theta d\theta$$

$$= 2 \int_0^{\frac{\pi}{2}} \sin^{2m-1} \theta \cos^{2n-1} \theta d\theta$$

$$\therefore I(9,14) + I(10,13) = 2 \int_0^{\frac{\pi}{2}} \sin^{17} \theta \cos^{27} \theta d\theta + 2 \int_0^{\frac{\pi}{2}} \sin^{19} \theta \cos^{25} \theta d\theta$$

$$= 2 \int_0^{\frac{\pi}{2}} \sin^{17} \theta \cos^{25} \theta (\cos^2 \theta + \sin^2 \theta) d\theta$$

$$= 2 \int_0^{\frac{\pi}{2}} \sin^{17} \theta \cos^{25} \theta d\theta$$

$$= I(9,13)$$

14. Let  $f(x) = \frac{2^{x+2} + 16}{2^{2x+1} + 2^{x+4} + 32}$  then  $f\left(\frac{1}{15}\right) + f\left(\frac{2}{15}\right) + \dots + f\left(\frac{59}{15}\right)$  is equal to

- (1) 28.25 (2) 29.25 (3) 29 (4) 30

Ans. (2)

Sol.  $f(x) = \frac{4(2^x + 4)}{2(2^{2x}) + 16(2^x) + 32}$

$$= \frac{2(2^x + 4)}{(2^x + 4)^2} = \frac{2}{2^x + 4}$$

$$\text{Now } f(x) + f(4-x) = \frac{2}{2^x + 4} + \frac{2}{2^{4-x} + 4} = \frac{2}{2^x + 4} + \frac{2 \times 2^x}{16 + 4 \times 2^x} = \frac{2}{2^x + 4} + \frac{2^x}{2(4 + 2^x)} = \frac{1}{2}$$

$$\text{So } f\left(\frac{1}{15}\right) + f\left(\frac{59}{15}\right) = \frac{1}{2}$$

$$f\left(\frac{2}{15}\right) + f\left(\frac{58}{15}\right) = \frac{1}{2}$$

$$\text{and } f\left(\frac{30}{15}\right) = \frac{2}{4+4} = \frac{1}{4} \text{ hence}$$

$$f\left(\frac{1}{15}\right) + f\left(\frac{12}{15}\right) + \dots + f\left(\frac{59}{15}\right) = 29 + \frac{1}{4} = 29.25$$

15. Let  $y(x)$  be the solution of differential equation  $\frac{dy}{dx} + \left(\frac{x}{1+x^2}\right)y = \frac{\sqrt{x}}{\sqrt{1+x^2}}$

If  $y(0) = 0$  then  $y(1)$  is equal to

- (1)  $\frac{2}{3}$  (2)  $\frac{2}{\sqrt{3}}$  (3)  $\frac{\sqrt{2}}{3}$  (4)  $\sqrt{\frac{2}{3}}$

Ans. (3)

Sol. I.F. =  $\int \frac{xdx}{1+x^2} = e^{\frac{1}{2}\ln(1+x^2)} = \sqrt{1+x^2}$

Solution of differential equation

$$y \cdot \sqrt{1+x^2} = \int \sqrt{1+x^2} \cdot \frac{\sqrt{x}}{\sqrt{1+x^2}} dx + C$$

$$y\sqrt{1+x^2} = \frac{2}{3}x^{3/2} + C$$

when  $x = 0, y = 0$  then  $C = 0$

so  $y = \frac{2x^{3/2}}{3\sqrt{1+x^2}}$  now at  $x = 1$

$$y = \frac{2}{3\sqrt{2}} = \frac{\sqrt{2}}{3}$$

16. Let  $f(x) - 6f\left(\frac{1}{x}\right) = \frac{35}{3x} - \frac{5}{2}$ , if  $\lim_{x \rightarrow 0} \left(\frac{1}{\alpha x} + f(x)\right) = \beta$

Then value of  $\alpha + 2\beta$  is

- (1) 0 (2) 1 (3) 3 (4) 4

Ans. (4)

Sol.  $f(x) - 6f\left(\frac{1}{x}\right) = \frac{35}{3x} - \frac{5}{2}$  .....(1)

Replace  $x \rightarrow \frac{1}{x}$

$$f\left(\frac{1}{x}\right) - 6f(x) = \frac{35x}{3} - \frac{5}{2}$$
 .....(2)

from (1) and (2)

$$f(x) = -2x - \frac{1}{3x} + \frac{1}{2}$$

Now

$$\beta = \lim_{x \rightarrow 0} \left(\frac{1}{\alpha x} - 2x - \frac{1}{3x} + \frac{1}{2}\right)$$

$$\Rightarrow \alpha = 3, \beta = \frac{1}{2}$$

So,  $\alpha + 2\beta = 3 + 1 = 4$

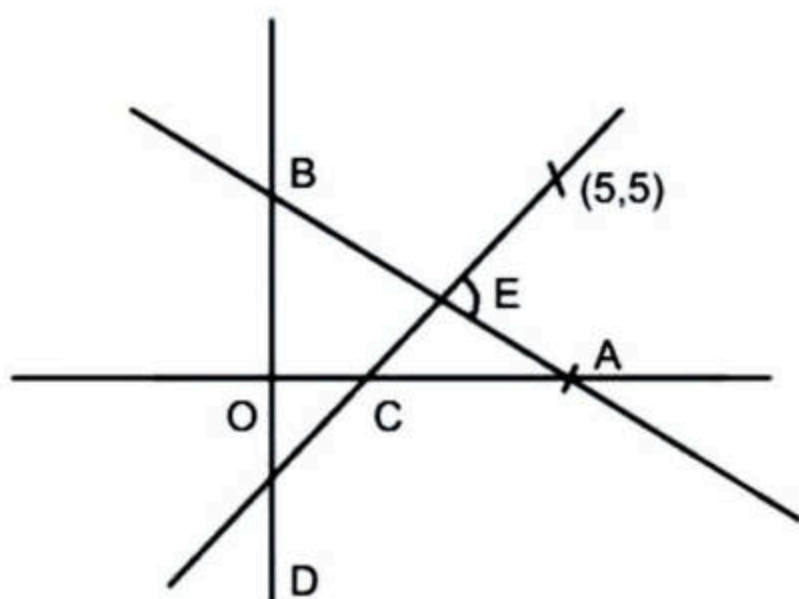
17. The line  $2x+3y = 12$  meets the x-axis at A and y-axis at B. The line through (5, 5), perpendicular to AB meets the x-axis, y-axis and AB at C, D and E respectively. If O is origin of coordinate axes then area of OCEB is

- (1)  $\frac{16}{3}$  (2)  $\frac{14}{3}$  (3)  $\frac{23}{3}$  (4)  $\frac{17}{2}$

Ans. (3)

Sol. A(6,0), B(0,4)  
AB is  $2x+3y = 12$   
ED is  $3x - 2y = 5$

Solving E (3,2), C( $\frac{5}{3}$ ,0) O(0,0)



$$\text{Area} = \frac{1}{2} \begin{vmatrix} 0 & \frac{5}{3} & 3 & 0 & 0 \\ 0 & 3 & 2 & 4 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{vmatrix} = \frac{1}{2} \left( \frac{10}{3} + 12 \right) = \frac{23}{3}$$

18. Let  $P(\sqrt{3}, \frac{1}{2})$  lies on ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , also product of focal distance of point P is  $\frac{7}{4}$  there are two ellipse satisfying given conditions then product of eccentricities is:

- (1)  $\left( \frac{1}{\sqrt{2}} \right)$  (2)  $\left( \frac{1}{2} \right)$  (3)  $\left( \frac{\sqrt{3}}{\sqrt{2}} \right)$  (4)  $\left( \frac{\sqrt{3}}{4} \right)$

Ans. (1)

Sol.  $PS_1 + PS_2 = 2a$  (i)  $P(\sqrt{3}, \frac{1}{2})$

$$PS_1 PS_2 = \frac{7}{4}$$

Squaring (i)  $PS_1^2 + PS_2^2 + 2PS_1 PS_2 = 4a^2$

$$(ae - \sqrt{3})^2 + \frac{1}{4} + (ae + \sqrt{3})^2 + \frac{1}{4} + 2 \cdot \frac{7}{4} = 4a^2$$

$$2a^2 e^2 + 10 = 4a^2$$

$$a^2 e^2 + 5 = 2a^2 \text{ (ii)}$$

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \text{ satisfying } \left( \sqrt{3}, \frac{1}{2} \right) \text{ in the equation}$$

$$\frac{3}{a^2} + \frac{1}{4b^2} = 1 \quad \{a^2 - a^2e^2 = b^2\}$$

$$\frac{3}{a^2} + \frac{1}{4a^2(1-e^2)} = 1$$

$$3 + \frac{1}{4(1-e^2)} = a^2 \quad \{\text{from (ii) } a^2 = \frac{5}{2-e^2}\}$$

$$3 + \frac{1}{4(1-e^2)} = \frac{5}{(2-e^2)}$$

$$12(1-e^2)(2-e^2) + (2-e^2) = 20(1-e^2)$$

Let  $1 - e^2 = t$

$$12t(1+t) + (1+t) = 20t$$

$$12t^2 + 12t + t + 1 = 20t$$

$$12t^2 - 7t + 1 = 0$$

$$(4t-1)(3t-1) = 0$$

$$t = \frac{1}{4} \quad \text{or} \quad t = \frac{1}{3}$$

$$1 - e^2 = \frac{1}{4} \quad \text{or} \quad 1 - e^2 = \frac{1}{3}$$

$$e^2 = \frac{3}{4} \quad \text{or} \quad e^2 = \frac{2}{3}$$

$$\text{so } e_1^2 \times e_2^2 = \frac{1}{2}$$

$$e_1 \times e_2 = \frac{1}{\sqrt{2}}$$

19. For ten observations  $x_1, x_2, x_3, \dots, x_{10}$ , mean is 5.5,  $\sum_{i=1}^{10} x_i^2 = 377$ , in which observations 4 and 5 are wrongly included. Replacing these wrong observations 4 and 5 by correct observations 6 and 8, then correct variance is:

- (1) 6.7                      (2) 8.7                      (3) 7.5                      (4) 7.6

**Ans. (4)**

**Sol.**  $x_1 + x_2 + \dots + x_8 + 4 + 5 = 55$  .....(1)

$x_1^2 + x_2^2 + \dots + x_8^2 + 4^2 + 5^2 = 377$  .....(2)

For corrected data mean is

$$\frac{x_1 + x_2 + \dots + x_8 + 6 + 8}{10} = \frac{55 - 9 + 6 + 8}{10} = 6$$

$$\sigma^2 + \bar{x}^2 = \frac{1}{n} \sum x_i^2$$

$$\sigma^2 + 6^2 = \frac{1}{10} (377 - 4^2 - 5^2 + 36 + 64)$$

$$= \frac{1}{10} (477 - 41) = \frac{436}{10} = \sigma^2 = 7.6$$